

Using the perceptual confirmation-bias to study learning and feedback in fovea and periphery

Ankani Chattoraj*, Richard D. Lange, Ralf M. Haefner*

Brain and Cognitive Sciences, University of Rochester, Rochester, NY 14627, USA

* {achattor,rhaefne2}@ur.rochester.edu

Abstract

When temporally integrating information, humans are often, but not always, biased to overweigh early evidence (“primacy effect”). We recently showed how these observations could be explained by assuming that the brain performs approximate inference in a hierarchical model in which expectations influence sensory inferences. Here, we use this framework to ask two related questions: (1) Does perceptual decision-making adapt to the rate at which new visual information is presented, or is its assumption fixed, learnt over long times? (2) Does the strength of feedback differ near the fovea compared to larger eccentricities, as in a recently proposed hypothesis?

In a first experiment, we compared the strength of the perceptual primacy effect in two conditions which only differed in the duration for which each stimulus frame was presented. We found that the primacy effect differed when measured in physical time, but stayed the same in “frame-time”, indicating that the brain had adapted to the rate at which it received independent information. Second, we compared the strength of the primacy effect near the fovea and in the periphery, and did not find a significant difference, suggesting an equal strength of feedback near the fovea and in the near periphery.

Keywords: perceptual decision-making; approximate inference; feedback; top-down

Introduction

Empirical studies show a wide variety in how subjects weigh evidence over time to make a perceptual choice. Sometimes subjects weigh early evidence more (“primacy effect”) (Nienborg & Cumming, 2009; Kiani, Hanks, & Shadlen, 2008), sometimes they weigh each piece of evidence equally (optimally) (Wyart, Gardelle, Scholl, & Summerfield, 2012; Brunton, Botvinick, & Brody, 2013), and sometimes they weigh later evidence more into their decision (“recency effect”) (Drugowitsch, Wyart, Devauchelle, & Koehlin, 2016) (Figure 1a). In a previous study (Lange, Chattoraj, Beck, Yates, & Haefner, 2018) we could explain these apparently conflicting results by making two contributions. First, given the fact that the brain’s decisions are always based on intermediate sensory inferences rather than the sensory observations (e.g. on the retina) directly, we showed that this implied a partitioning of total information available in the stimulus into “sensory information” (the information in each observation about the sensory inference) and “category information” (the information in each inference is about the correct choice). The

different relative proportions of sensory and category information were predictive of the experimental findings, with primacy effects (decreasing psychophysical kernels, or PKs) occurring for low sensory and high category information. Second, we showed that approximate inference in a hierarchical generative model predicts these different temporal biases depending on relative sensory and category information (Figure 1c and stimulus in 1d). For our present study, we concentrate on the regime of low sensory information and high category information. In this regime, our model makes testable predictions for how the strength of the primacy effect should depend on (1) the assumptions of the brain about the rate at which it receives independent information, and (2) on the strength of the feedback connections with which prior expectations influence sensory inferences in our model.

Results

Study 1: Does the brain adapt its assumptions about the temporal correlations in the stimulus to the stimuli in different tasks?

On a given trial, if the evidence in frame f is e_f and the (correct) categorical identity of the stimulus is a binary variable $C \in \{-1, +1\}$, then evidence in favor of $C = +1$ after F independent frames is:

$p(C = +1|e_1, \dots, e_F) \propto p(C = +1) \prod_{f=1}^F p(e_f|C = +1)$. In the case of the brain, a decision-making area computing a belief about the correct choice only has access to a sensory representation of the stimulus, which we call x , not to the outside stimulus e directly (Figure 1b and c). As in the Sequential Probability Ratio Test (Gold & Shadlen, 2007), we assume the brain approximately computes beliefs about the correct choice as

$$\begin{aligned} \underbrace{\log \frac{\text{pr}(C = +1)}{\text{pr}(C = -1)}}_{\text{LPO}_f} &\equiv \log \frac{p(C = +1|e_1, \dots, e_f)}{p(C = -1|e_1, \dots, e_f)} \\ &= \log \frac{\text{pr}_{f-1}(C = +1)}{\text{pr}_{f-1}(C = -1)} + \log \frac{p(e_f|C = +1)}{p(e_f|C = -1)} \\ &= \underbrace{\log \frac{\text{pr}_{f-1}(C = +1)}{\text{pr}_{f-1}(C = -1)}}_{\text{LPO}_{f-1}} + \underbrace{\log \frac{\int_x p(e_f|x)p(x|C = +1)dx}{\int_x p(e_f|x)p(x|C = -1)dx}}_{\text{LLO}_f} \\ &= \text{LPO}_{f-1} + \text{LLO}_f \end{aligned} \quad (1)$$

where LLO_f is the decision-making area’s estimate of the log-likelihood ratio implied by evidence frame f , using the



approximate sensory representation x (for details see (Lange et al., 2018)). Presumably the decision-making area updates its belief about C continuously, reflecting the rate of the brain's underlying computations, and without any knowledge about experimenter-controlled frame-by-frame changes in the externally presented stimulus. We therefore introduced a parameter n_U for the number of online belief updates by the decision-making area per stimulus frame. As a result we have to amortize the per-frame updates over n_U steps, updating n_U times per frame; i.e. $\hat{L}\hat{L}O_f = \sum_{i=1}^{n_U} \frac{1}{n_U} \hat{L}\hat{L}O_f^{(i)}$. This amortization coefficient $1/n_U$ reflects a fundamental complication in applying the sequential ratio test (SRT) to continuous inputs from the real world: while the SRT is the correct solution for truly independent pieces of evidence, stimuli in the outside world are usually correlated over time, whether they are consecutive views of the same scene, or consecutive newspaper articles on the same topic. In agreement with intuition, our model of approximate hierarchical inference predicts that the stronger the assumption that external stimuli (in our case the images on the screen) are independent pieces of information, the stronger the primacy effect, and vice versa. In the context of our modeled experiment, a stronger independence assumption means that the brain assumes a smaller number of sensory updates n_U per independent piece of external evidence. Optimal performance requires that it learns the correct n_U . Whether the brain can do so in a context-dependent during perceptual decision-making, or whether it uses an approximate n_U learnt during natural vision, is the question addressed by our first experiment.

Visual Discrimination Task Following (Lange et al., 2018), the stimulus in our task consisted of ten visual frames. Each frame consisted of band-pass-filtered noise with excess orientation power either in the -45deg or the $+45\text{deg}$ orientation (Nienborg & Cumming, 2014) (Figure 1d). Here, the excess orientation power, parameterized by $0 \leq \kappa < \infty$ (parametrizing a von-Mises filter function in orientation space), determines the uncertainty over orientation for each frame (sensory information). The stimulus was presented as an annulus spanning 2.088 degrees around the fixation marker in order to minimize the effect of small fixational eye movements (inner circular mask spans 0.432 degrees around fixation, see Figure 1d). Subjects reached threshold performance using a 2-1 staircase decreasing κ . We compared two variations of this experiment: in one, the duration of each evidence frame was 42 msec, and in the other case it was 166 msec.

Findings Figure 1f-g shows our model predictions for three different stimulus frame durations ($n_U = 5, 10, 20$) measured in how many online updates the brain performs for a single stimulus frame, e_f . Figure 1f shows the case in which the brain has learnt the correct amortization factor, $1/\tau = 1/n_U$: the strength of the primacy effect (slope of the weights as a

function of independent stimulus frame) is always the same. Figure 1g shows the results assuming the brain uses the same amortization constant no matter for how long each independent frame was presented ($1/\tau \neq 1/n_U$): the slope is steeper for longer than for shorter frames. Figure 2a,b,e,f,g show our empirical data from 10 subjects (9 naive). When comparing the weights as a function of the independent frame number, the average slope is the same in both condition (Figure 2a+b) as in agreement with the hypothesis that the brain has changed its amortization constant by a factor of 4 to account for the different frame durations in both cases. If, however, the brain had kept its amortization constant the same across both conditions, the weights should have declined with the same slope when measured in physical time – in clear contradiction of the data (Figure 2a and e). Finally, we note that the clear primacy effect even over the relatively short stimulus duration of 420ms (Figure 2e+f) provides additional evidence (beyond that already in (Lange et al., 2018)) against an internal integration-to-bound process as an explanation for the observed primacy effect.

Study 2: Is the strength of the feedback signals different near fovea and in the periphery?

A key driver of the primacy effect in our model and – we propose – in the brain, is the fact that sensory inferences incorporate top-down prior expectations. If this was not the case, then even under the assumption of approximate inference, our model would never predict a primacy effect and the predicted slope would be zero. Recently, it was proposed (Zhaoping & Ackermann, 2018; Zhaoping, 2017) that the strength of feedback is greater in and near the fovea than in the periphery. We tested this hypothesis by comparing the strength of the primacy effect (quantified by the slope of the weights) for two stimuli that varied in eccentricity but were matched in all other aspects relevant for the model. In particular, we scaled the area that the stimulus occupied on the screen with the cortical magnification factor (Strasburger, Rentschler, & Jüttner, 2011). We equivalently scaled the spatial frequency content of the stimulus in order to account for the dependence of the spatial frequency preferences of cortical neurons on eccentricity (Strasburger et al., 2011). These manipulations ensured that the number of cortical visual neurons processing the the stimuli in the two conditions stayed roughly the same since their number may affect the quality of the sensory representation and hence the strength of the primacy effect.

Visual Discrimination Task We had 7 naive subjects perform the same visual discrimination task as in Study 1 above and described in (Lange et al., 2018) with the following parameters. Independent stimulus frames of duration 83ms were presented in both conditions. In the condition 1, the stimulus had the same size as before, an annulus of size 2.088 degrees around the fixation marker (inner circular

mask spans 0.4352 degrees around fixation). In condition 2, the stimulus was a larger annulus spanning 3.24 degrees and the inner circular mask spans 2.088 degrees around the fixation cross (Figure 1d+e). Spatial frequency peaked at 0.1194 cycles/pixel for the small stimulus, compared to 0.0980 cycles/pixel for the large stimulus.

Findings Figure 1h shows our model predictions for the change in the strength of top-down feedback signals from decision-making area to the sensory representation. We confirm in our model simulations that an increase in feedback strength implies a stronger primacy effect. Hence, if the feedback signals near fovea are stronger than in the periphery we would expect to see a stronger primacy effect for trials with stimuli near the fovea than for trials with stimuli in the periphery. Figure 2c-d shows our data from 7 naive subjects across the two conditions indicating no significant difference between the slopes of the weighting profiles for the two types of stimuli. This suggests that the strength of the feedback signals in the periphery are similar to that near fovea at over the range of eccentricities tested by our experiment.

during Decision Making in the Human Brain. *Neuron*, *76*(4), 847–858.

Zhaoping, L. (2017). Feedback from higher to lower visual areas for visual recognition may be weaker in the periphery: Glimpses from the perception of brief dichoptic stimuli. *Vision research*, *136*, 32–49.

Zhaoping, L., & Ackermann, J. (2018). Reversed depth in anticorrelated random-dot stereograms and the central-peripheral difference in visual inference. *Perception*, *47*(5), 531–539.

References

- Brunton, B. W., Botvinick, M. M., & Brody, C. D. (2013). Rats and humans can optimally accumulate evidence for decision-making. *Science*, *340*(6128), 95–8.
- Drugowitsch, J., Wyart, V., Devauchelle, A.-D., & Koechlin, E. (2016). Computational Precision of Mental Inference as Critical Source of Human Choice Suboptimality. *Neuron*, *92*(6), 1398–1411.
- Gold, J. I., & Shadlen, M. N. (2007). The neural basis of decision making. *Annual review of neuroscience*, *30*(30), 535–574.
- Kiani, R., Hanks, T. D., & Shadlen, M. N. (2008). Bounded integration in parietal cortex underlies decisions even when viewing duration is dictated by the environment. *The Journal of neuroscience*, *28*(12), 3017–3029.
- Lange, R. D., Chattoraj, A., Beck, J., Yates, J., & Haefner, R. (2018). A confirmation bias in perceptual decision-making due to hierarchical approximate inference. *bioRxiv*, 440321.
- Nienborg, H., & Cumming, B. G. (2009). Decision-related activity in sensory neurons reflects more than a neuron's causal effect. *Nature*, *459*(7243), 89–92.
- Nienborg, H., & Cumming, B. G. (2014). Decision-related activity in sensory neurons may depend on the columnar architecture of cerebral cortex. *The Journal of neuroscience*, *34*(10), 3579–85.
- Strasburger, H., Rentschler, I., & Jüttner, M. (2011). Peripheral vision and pattern recognition: A review. *Journal of vision*, *11*(5), 13–13.
- Wyart, V., Gardelle, V. D., Scholl, J., & Summerfield, C. (2012). Rhythmic Fluctuations in Evidence Accumulation

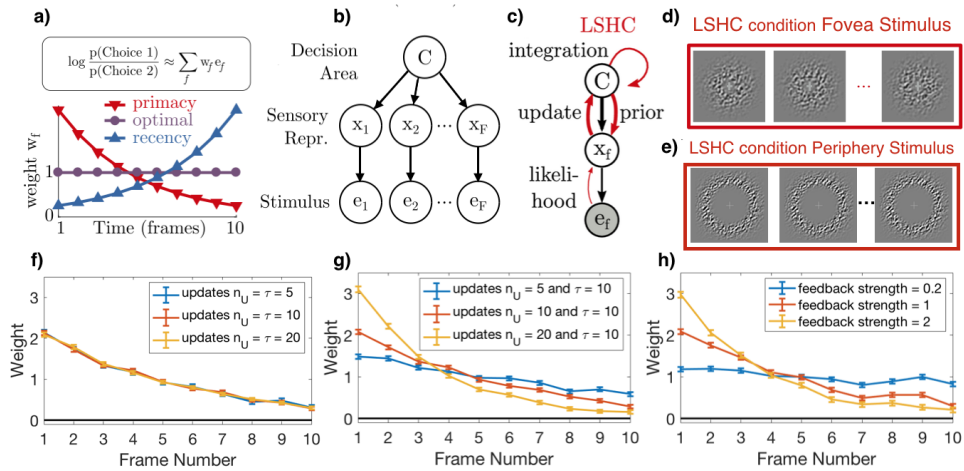


Figure 1: Predictions from Sampling-based Inference Model for Visual Discrimination Task

a) Possible temporal weight profiles for evidence integration tasks. **b)** The generative model of time-changing external evidence, e_t . The category is denoted by C and the sensory representation in the brain is x_t . **c)** Approximate inference model: Red lines show information flow with our assumption that a posterior over x_t is represented and evidence integration happens in a decision area representing C . Strong feedback from C to x gives primacy weighting. **d)** Example band-passed grating stimulus where all frames contain noisy information about one category used in Study 1 and fovea stimulus for Study 2. **e)** Same as (d) used as periphery stimulus in Study 2. **f)** Model Simulations: When the amortization factor τ matches number of belief updates per frame of evidence n_U , then there is no change in slope of weights (strength of primacy) with change in n_U . **g)** If $\tau \neq n_U$, then primacy strengthens with increase in number of belief updates n_U . **h)** Stronger top-down feedback from C to x gives stronger primacy weighting.

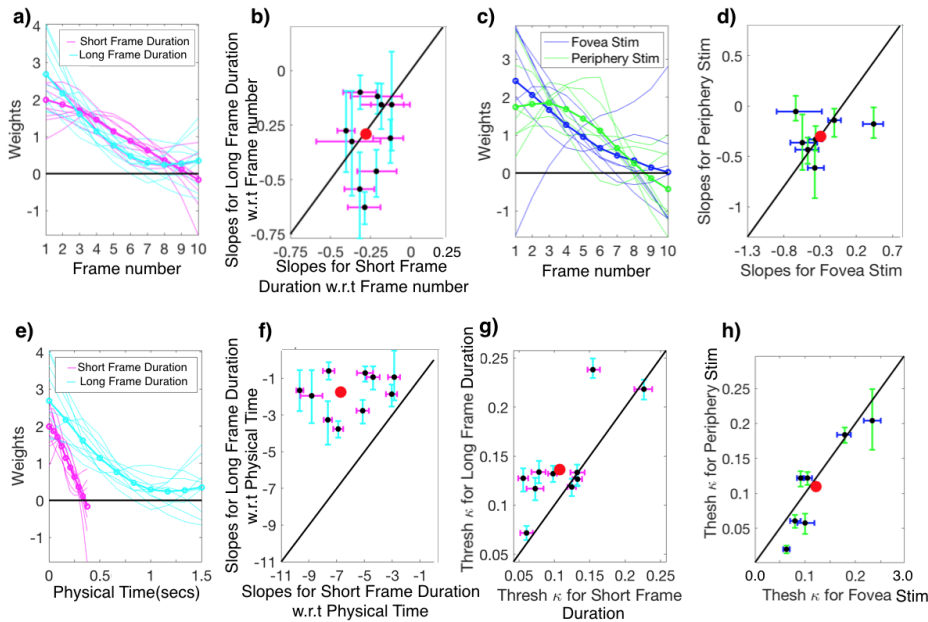


Figure 2: Empirical Data for Study1 and Study2

a) Primacy in weighting across frame number for 10 subjects in Study1. **b)** No significant difference in slope of the weighting profiles when averaged across all subjects (red dot), for the two conditions in Study1. **c)** Primacy in weighting across frame number for 7 subjects in Study2. **d)** Same as (b) but for Study2. **e)** Steeper weighting profile in trials with short stimulus frame duration when plotted w.r.t physical time. **f)** Scatter plot for slopes of the weighting profiles in (e). **g)** The κ corresponding to 70% performance across subjects is approximately the same for the two conditions of Study 1. **h)** Same observation as in (g) but for Study 2.